

FMM Petrel Plug-In (Fast Marching Method)

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Outline

- Motivation
- Background
- FMM-plug in
 - FMM plug-in Features
 - Plug-in Workflow
- Demonstration

Motivation

- Drainage volume and pressure depletion are important in unconventional reservoirs
- Quickly generalize the concept of drainage volume to account for complex geologic stratigraphy, reservoir heterogeneity and well/fracture geometry

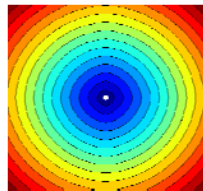
Background

Pressure Front Propagation

Radius of Investigation (ROI)
for **homogeneous** reservoir

$$r = \sqrt{\frac{4kt}{\phi\mu c_i}}$$

'Peak' arrival time
(Impulse source)



(Lee, 1982)

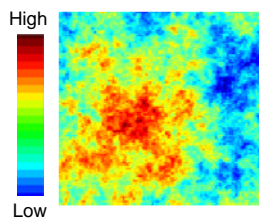
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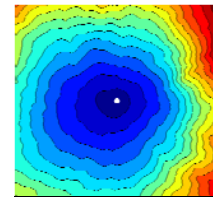
Generalization of ROI
for **heterogeneous** reservoir

Eikonal eq.: $\sqrt{\frac{k(\mathbf{x})}{\phi(\mathbf{x})\mu c_i}} |\nabla \tau| = 1$

Speed (diffusivity)



Diffusive Time-of-Flight



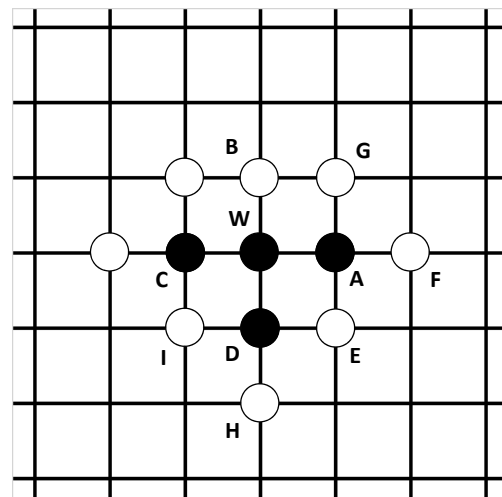
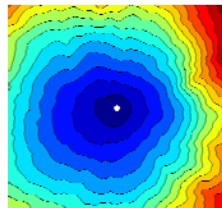
(Datta-Gupta et. al., 2011)

Travel Time Calculations by Fast Marching Method

Fast Marching Method (FMM)*

- Efficiently solves eikonal eq. for Diffusive Time-of-Flight τ (DTOF)
- Sequential calculation of shortest path from a source outwards

Diffusive Time-of-Flight Map

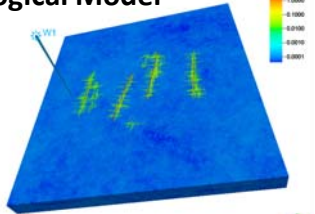


*Dijkstra (1959), Sethian (1996)

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Application to Unconventional Reservoirs: Drainage Volume Calculation Using Fast Marching Method

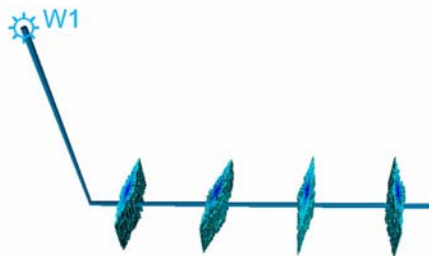
Geological Model



Fracture System

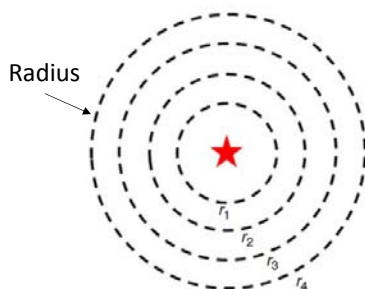


Drainage Volume

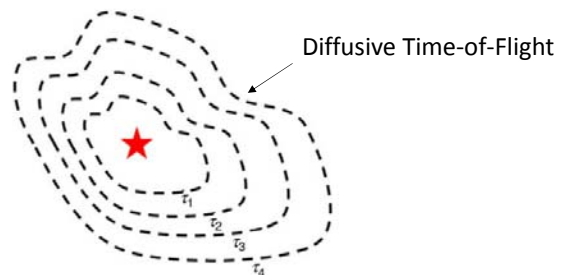


Generalization of Radial Diffusivity Equation Using Diffusive Time-of-Flight as a 1-D Spatial Coordinate

Homogeneous reservoir



Heterogeneous reservoir

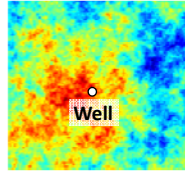


$$\frac{k}{\phi \mu c_t} \frac{1}{r} \frac{\partial}{\partial r} \left(r \frac{\partial P}{\partial r} \right) = \frac{\partial P}{\partial t} \quad \xrightarrow{r \rightarrow \tau} \quad \frac{1}{w(\tau)} \frac{\partial}{\partial \tau} \left(w(\tau) \frac{\partial P}{\partial \tau} \right) = \frac{\partial P}{\partial t}$$

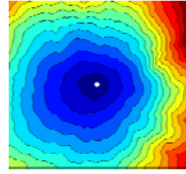
$$w(\tau) = \frac{dV_p(\tau)}{d\tau}$$

Rapid Simulation of Unconventional Reservoirs: 3-D to 1-D Formulation

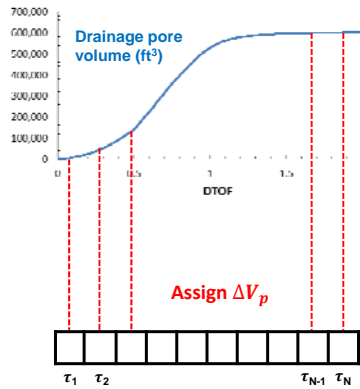
Spatial Heterogeneity



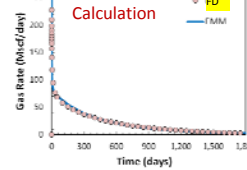
FMM



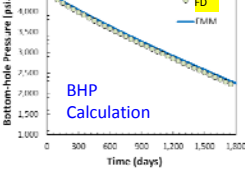
Drainage Volume



Rate Calculation



BHP Calculation



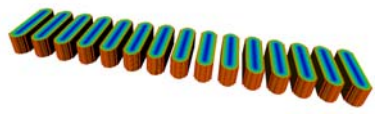
Numerical Flow Simulation

1-D τ -coordinate

CPU Time: Orders of Magnitude Faster Computation than Commercial FD Simulator

Significant gain in computational efficiency

- Dual Porosity Model, Horizontal well with 15 HFs
- BHP constraint
- 20 years forecast

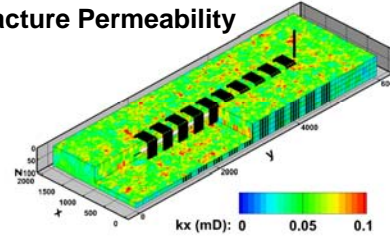


	Cell number (millions)	CPU Finite Difference(s)	CPU FMM (s)	Ratio
Base	1.03	574.7	13.1	43.87
High k_f	1.03	557.9	13.1	42.59
High k_m	1.03	691.6	13.2	52.40
Long x_f	1.03	596.2	13.4	43.75
More stages	1.23	628.0	16.4	38.29

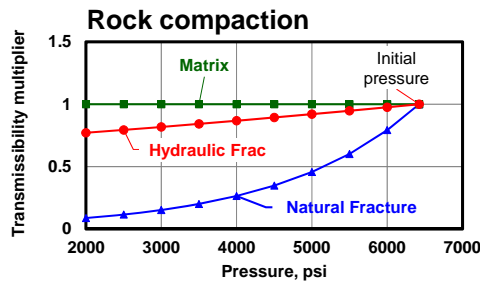
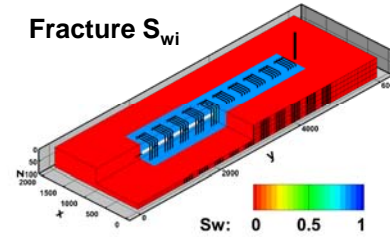
Rapid Compositional Simulation Using Fast Marching Method

- 0.4 million cells with reservoir heterogeneity
- Multi-stage hydraulic fractures
- 3-phase and 7-component
- Dual-porosity
- High water saturation around well
- Permeability reduction due to compaction
- Primary depletion + CO₂ Huff-n-Puff (5-cycle)

Fracture Permeability



Fracture S_{wi}

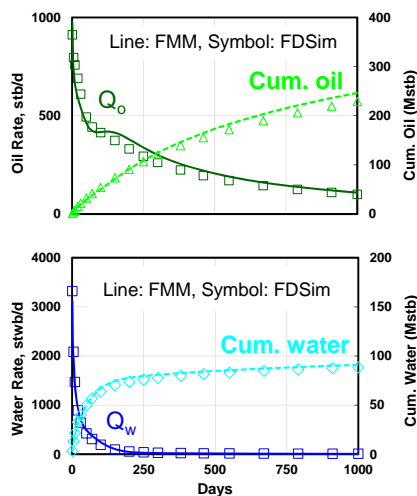


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Simulation Results

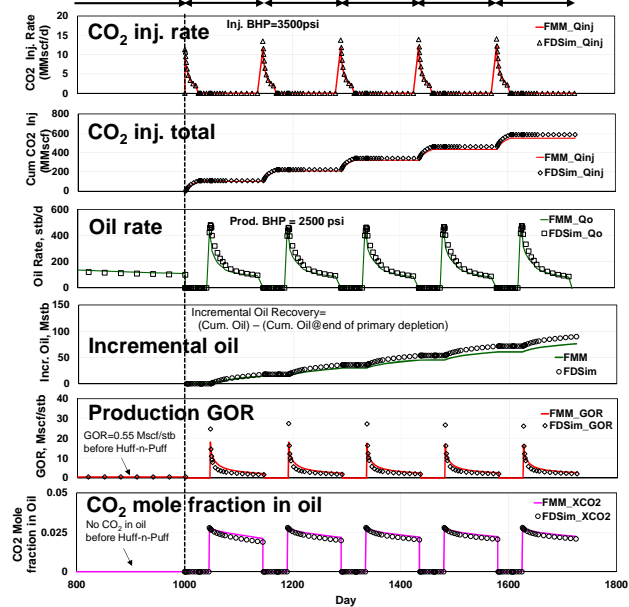
Speed-up factor x 320
(compared to commercial FD simulator)

Primary depletion



CO₂ Huff-n-Puff

32% increase in incremental oil
than do-nothing case

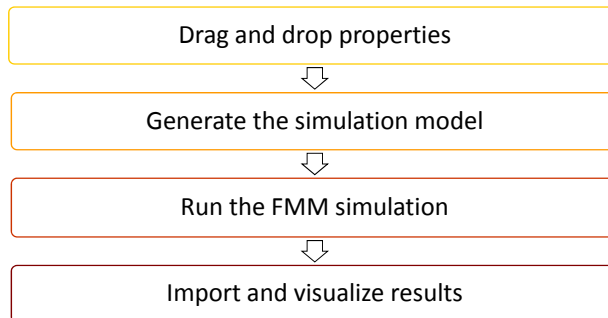


FMM Petrel Plug-in

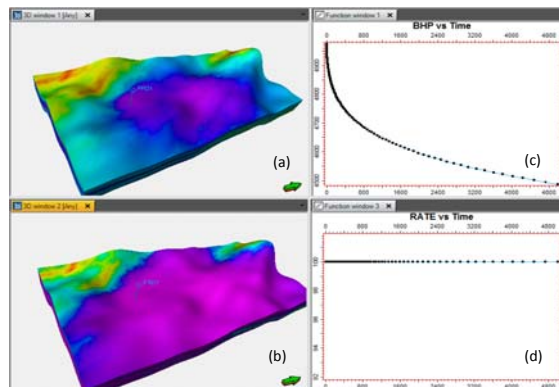
FMM Plug-in Features

- Current version
 - Drainage volume calculation (single-phase)
 - 1-D simulation (single-phase)
- Future plan
 - Multi-phase black oil simulation
 - Compositional simulation

FMM Petrel Plug-in Workflow

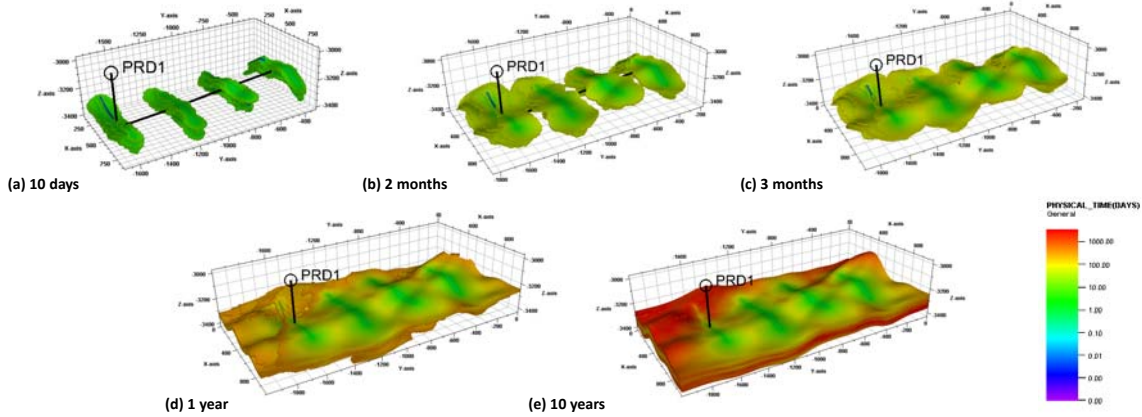


Visualizing Results in Petrel

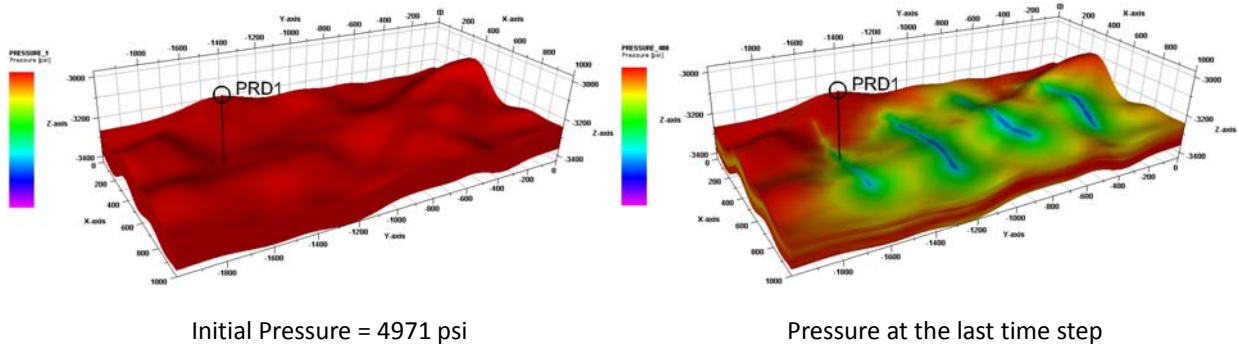


(a) Diffusive Time of Flight; (b) Drainage Volume; (c) BHP; (d) Rate

Evolution of Drainage Volume with Time

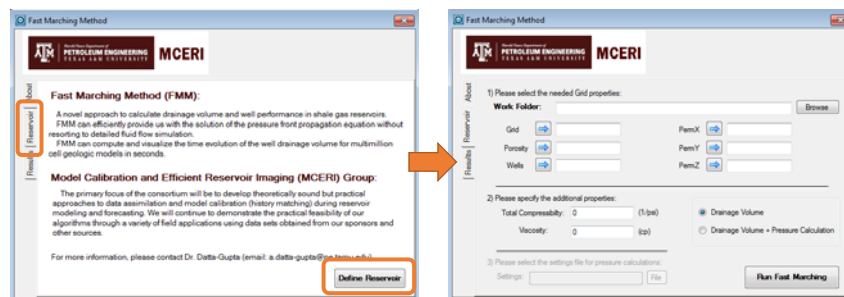


Visualizing Pressure on the Grid



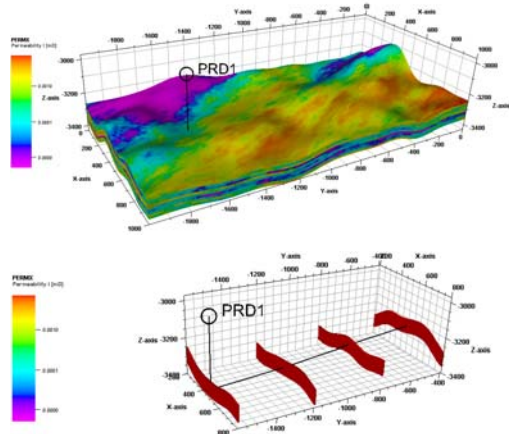
Training Session : Petrel Plug-in

FMM Petrel Plug-in User Interface

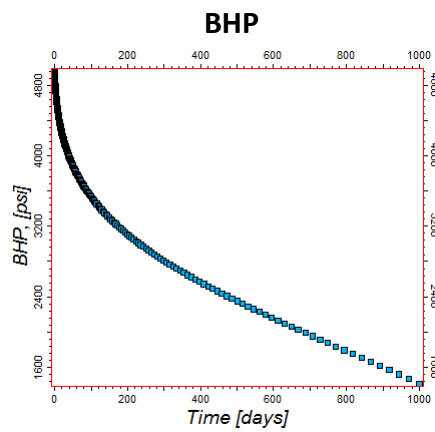
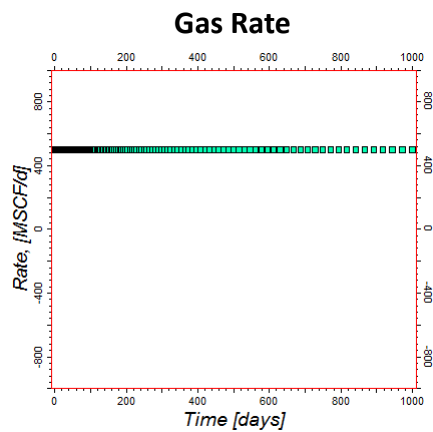


Model for Demonstration

Reservoir dimension	1000 ft x 2000 ft x 120 ft	
The number of grid blocks	100 x 200 x 10	
Well data	1 Producer Horizontal Well	Rate constrained : 500 MSCF/D
Hydraulic Fractures (4)	Half Length	300 ft
	Width	2 ft
Porosity	0.05	
Permeability	Matrix	Avg. $k_h = 7.23e-4$ md $k_x = k_y \frac{k_v}{k_h} = 0.1$
	Fracture	100 md

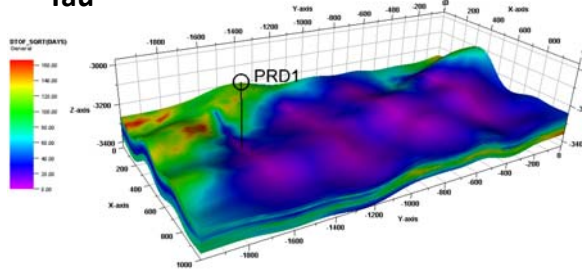


Results from Democase

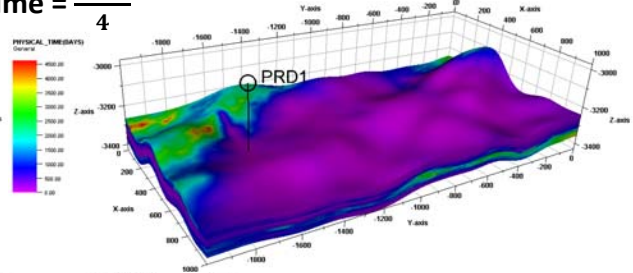


Results from Democase

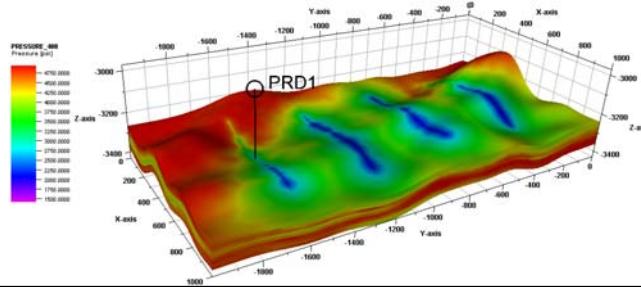
Tau



$$\text{Time} = \frac{\text{Tau}^2}{4}$$



Pressure



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